

$$\lim_{n \rightarrow +\infty} (\sqrt{n^3+3n+1} - \sqrt{n^3+3n-1}) n^{\frac{1}{6}} (\sqrt[3]{n^2-1})^2 =$$

ZT 16/17
VAR B

$$= \lim_{n \rightarrow +\infty} (\sqrt{n^3+3n+1} - \sqrt{n^3+3n-1}) \left[\frac{\sqrt{n^3+3n+1} + \sqrt{n^3+3n-1}}{\sqrt{n^3+3n+1} + \sqrt{n^3+3n-1}} \right] n^{\frac{1}{6}} (\sqrt[3]{n^2-1})^2 =$$

$$= \lim_{n \rightarrow +\infty} \frac{n^3+3n+1 - (n^3+3n-1)}{\sqrt{n^3+3n+1} + \sqrt{n^3+3n-1}} n^{\frac{1}{6}} (\sqrt[3]{n^2-1})^2 = \lim_{n \rightarrow +\infty} \frac{2 n^{\frac{1}{6}} (n^{\frac{2}{3}} \sqrt[3]{1-\frac{1}{n^2}})^2}{n^{\frac{3}{2}} \left[\sqrt{1+\frac{3}{n^2}+\frac{1}{n^3}} + \sqrt{1+\frac{3}{n^2}-\frac{1}{n^3}} \right]} =$$

$$= \lim_{n \rightarrow +\infty} \frac{2 n^{\frac{1}{6}} n^{\frac{4}{3}} (\sqrt[3]{1-\frac{1}{n^2}})^2}{n^{\frac{3}{2}} \left[\sqrt{1+\frac{3}{n^2}+\frac{1}{n^3}} + \sqrt{1+\frac{3}{n^2}-\frac{1}{n^3}} \right]} = \frac{2 (\sqrt[3]{1})^2}{\sqrt{1} + \sqrt{1}} = \frac{2}{2} = 1$$

$$\left(n^{\frac{1}{6}} \cdot n^{\frac{4}{3}} = n^{\frac{1+8}{6}} = n^{\frac{9}{6}} \right)$$